



Two Topics in Higgs Physics

JAE SIK LEE

Chonnam National University, Gwangju

17–23 August, 2016 @ SI2016, Taiwan



Two Topics

1. Unitarity in W - b scattering
2. Almost degenerate Higgses

Unitarity in W - b scattering

It's about charged Higgs production in 2HDMs

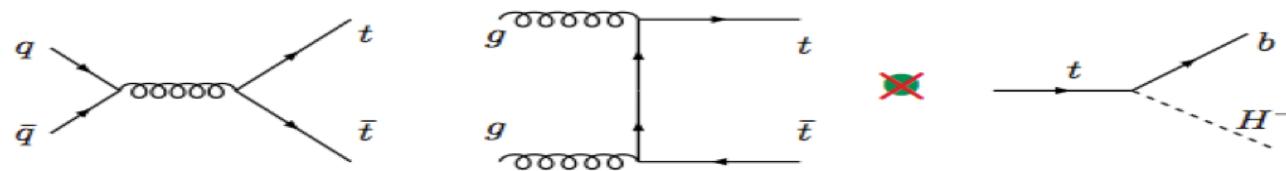
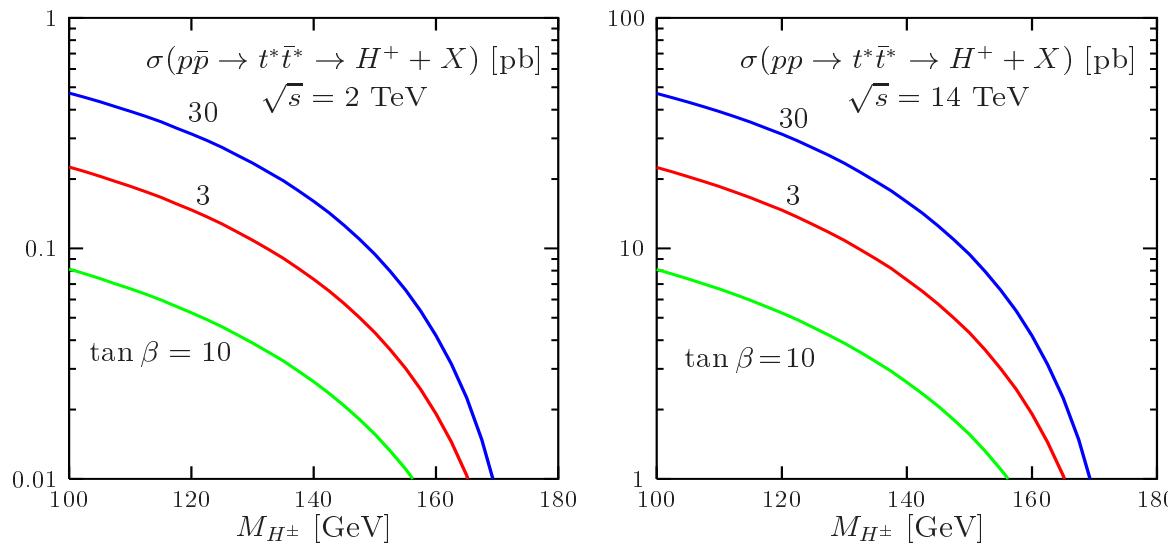
* based on A. Arhrib, K. Cheung, JSL, C.-T. Lu, JHEP 1605 (2016) 093 [arXiv:1509.00978]



Preliminary

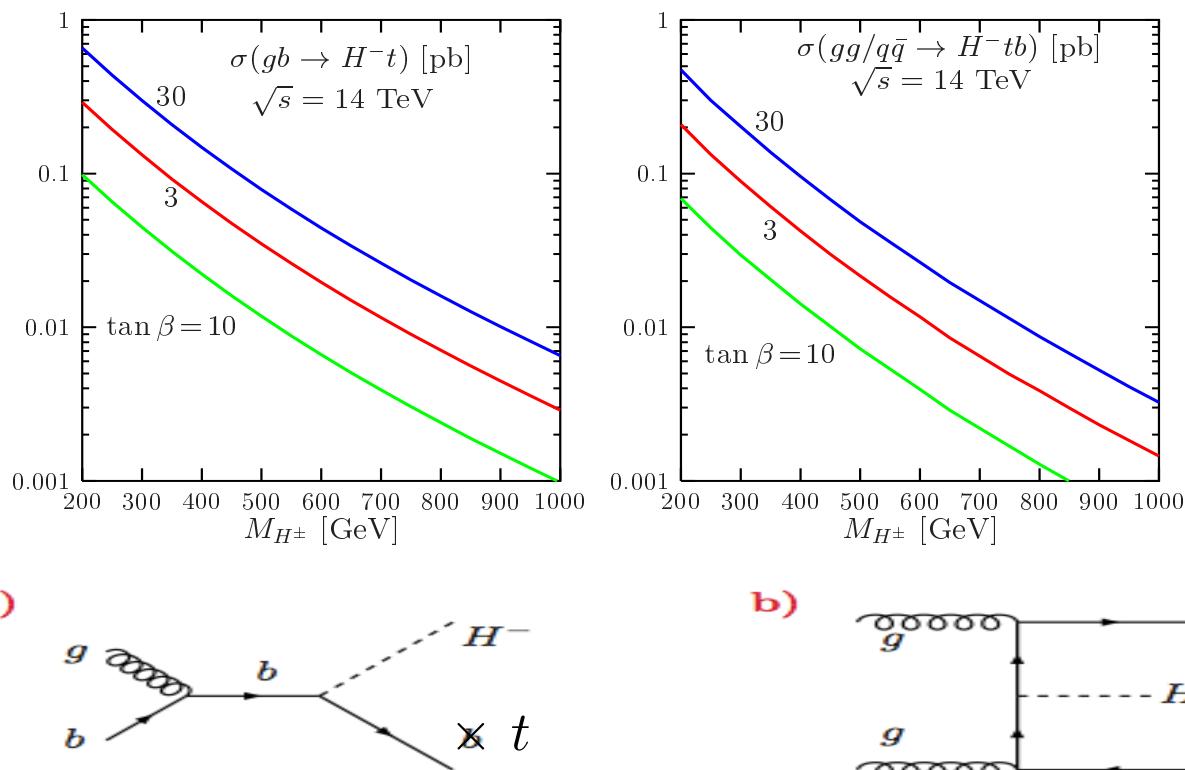
- The production of the charged Higgs bosons [The Anatomy of electro-weak symmetry breaking. II. The Higgs bosons in the minimal supersymmetric model : Abdelhak Djouadi Phys.Rept. 459 \(2008\) 1-241, hep-ph/0503173](#)
 - Production from top quark decays
 - The gb and gg fusions
 - The single charged Higgs production process
 - The pair and associated production processes

- Production from top quark decays: $M_{H^\pm} \lesssim m_t$



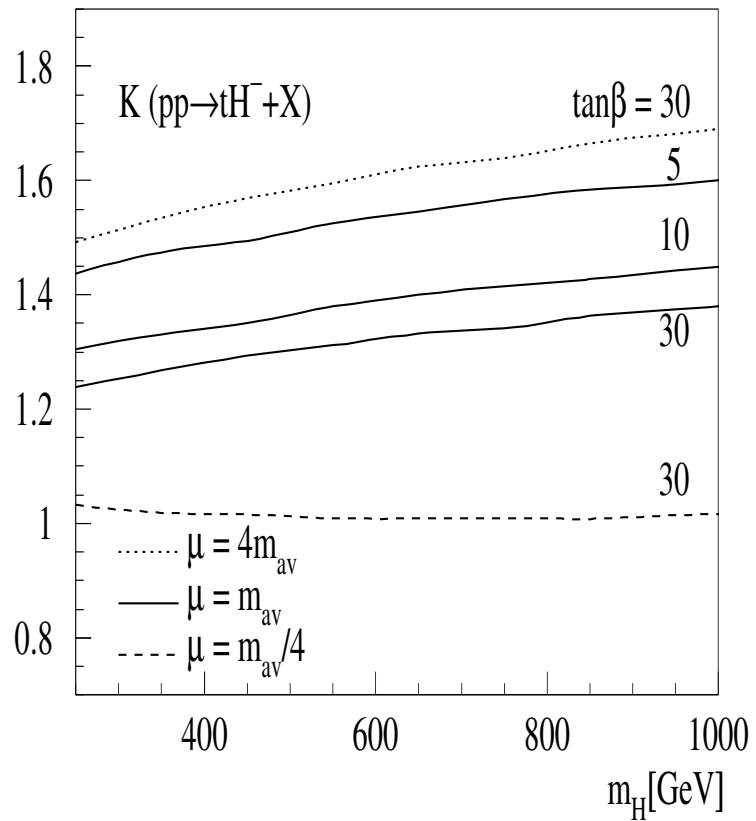
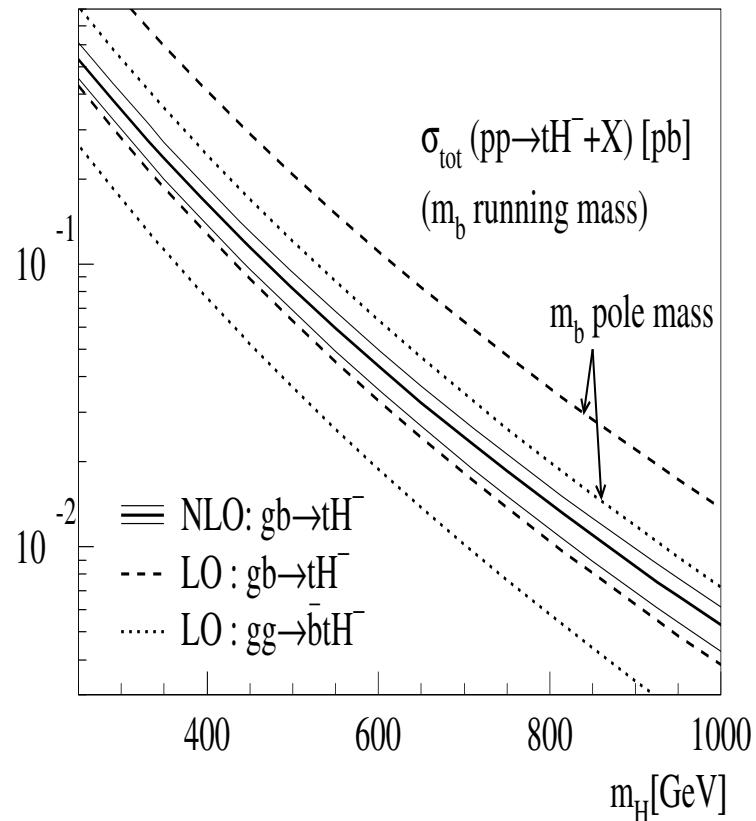
♠ Preliminary

- The gb and gg fusions in LO: $M_{H^\pm} \gtrsim m_t$



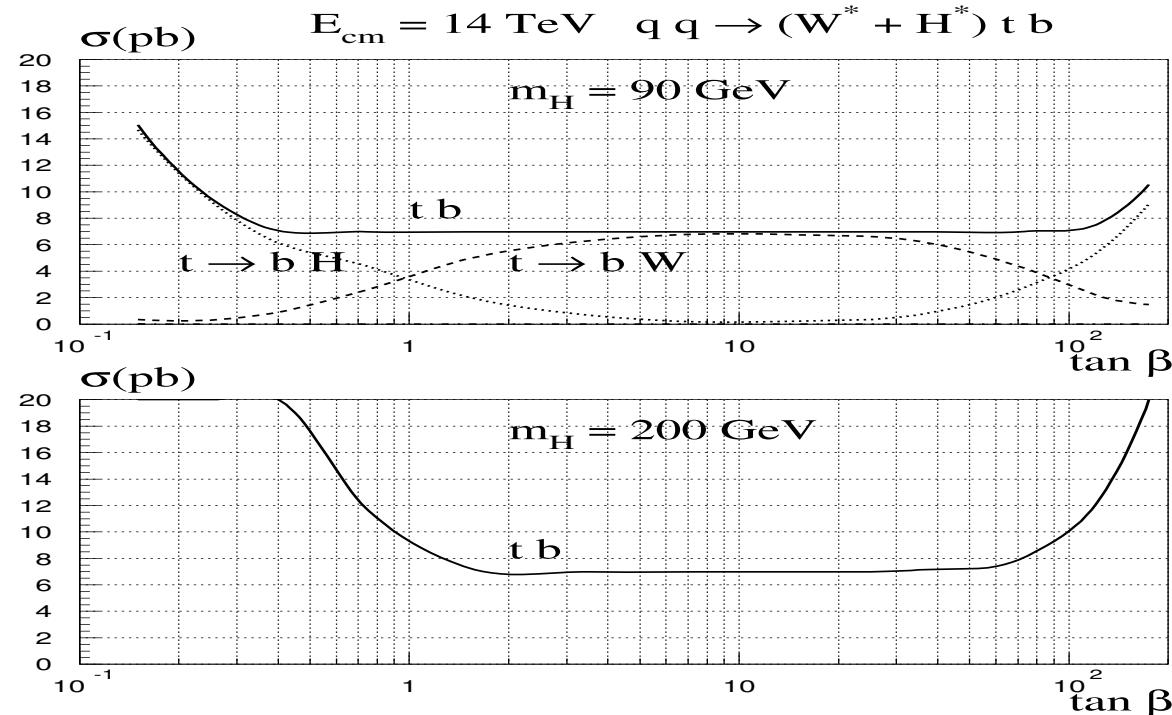
In fact, the process $gg \rightarrow H^- t\bar{b}$ is in fact simply part of the NLO QCD corrections to $gb \rightarrow H^- t$ when the momentum of the additional final b quark is integrated out

- The gb fusion: $M_{H^\pm} \gtrsim m_t$ NLO corrections with $m_{av} = (m_t + M_{H^\pm})/2$

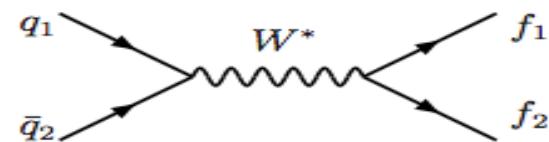


♠ Preliminary

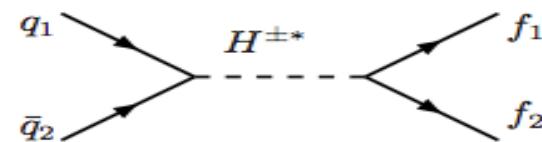
- The single production: $pp \rightarrow tb, \tau\nu$ huge background extremely difficult



a)

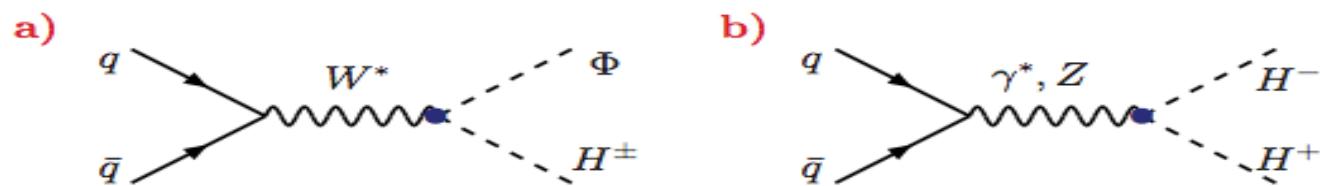
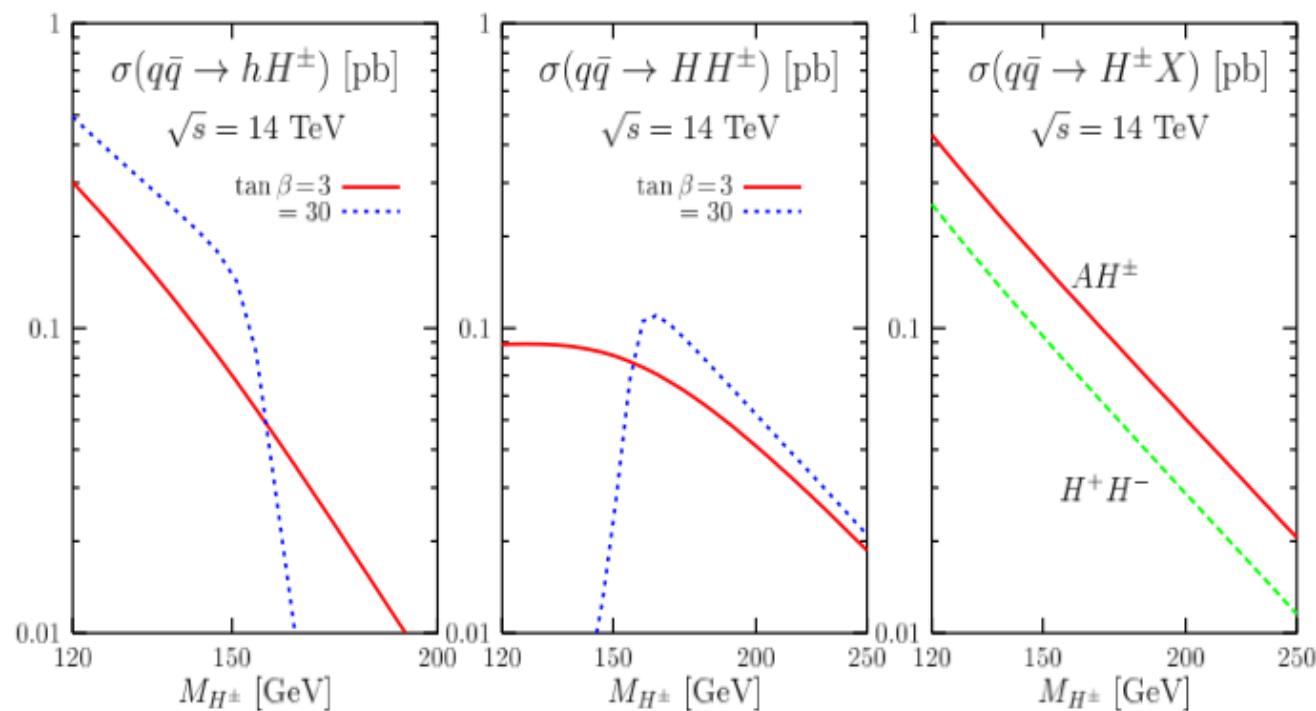


b)

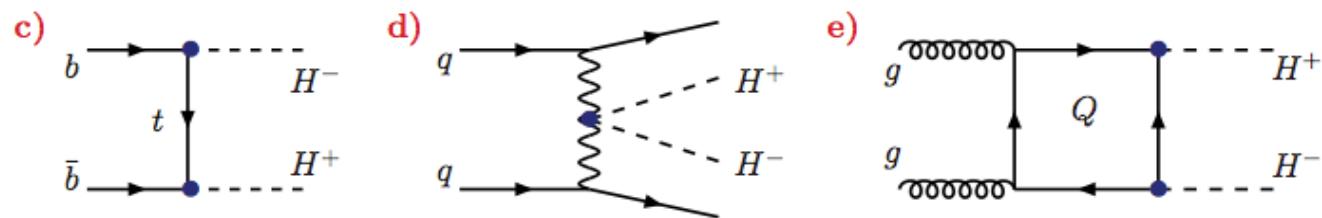
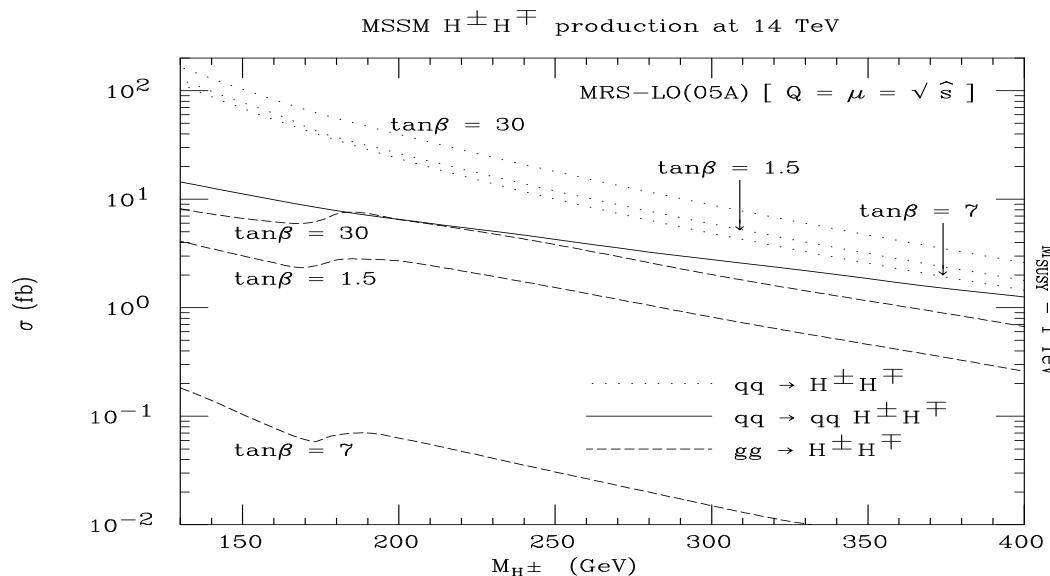


♠ Preliminary

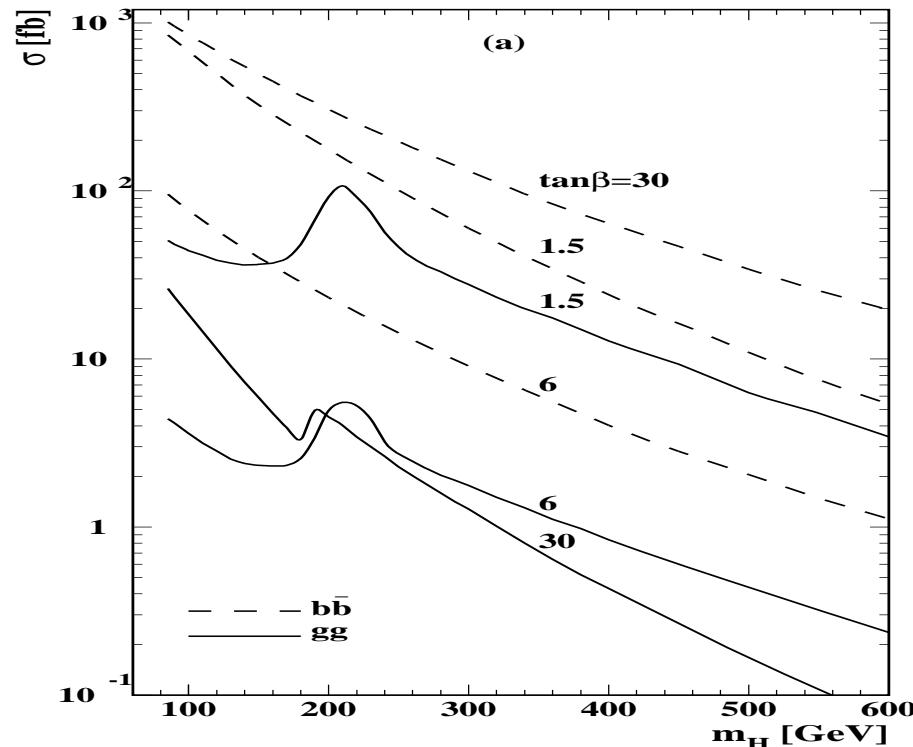
- The pair production 1: $g_{H_i VV}^2 + |g_{H_i H^+ W^-}|^2 = 1$ for each i



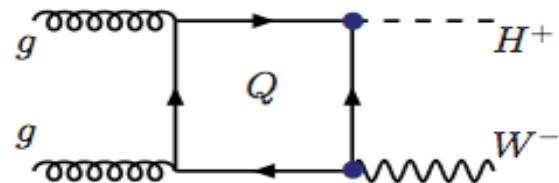
- The pair production 2:



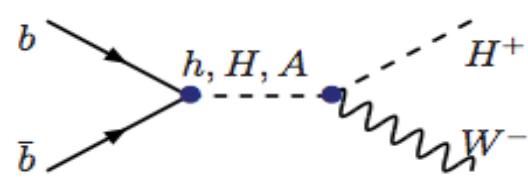
- The associated production:



f)



g)



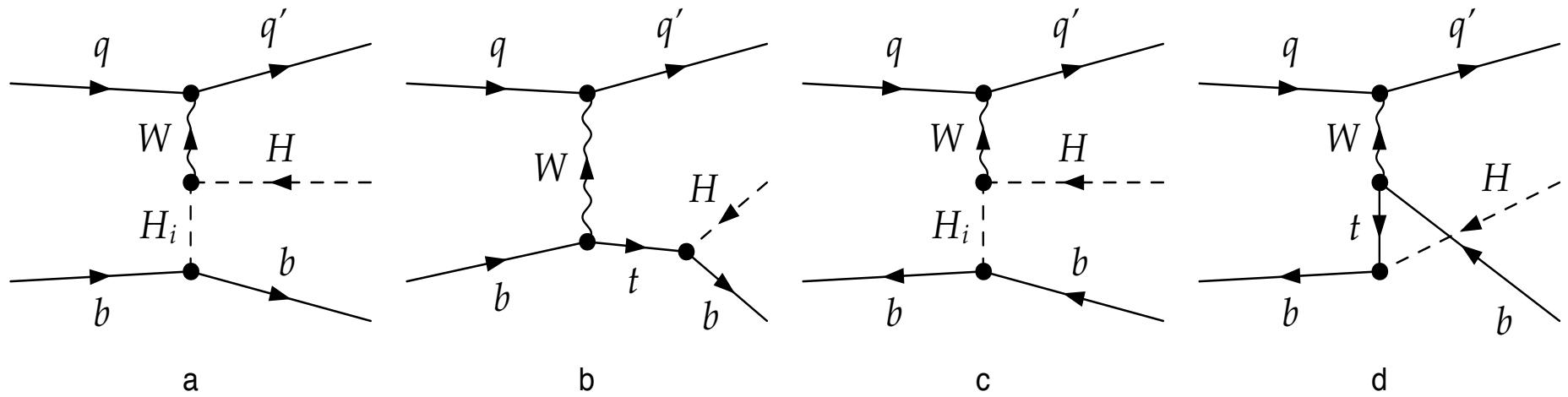


Preliminary

- A very brief summary:
 - $M_{H^\pm} \lesssim m_t$: $\sigma(q\bar{q}, gg \rightarrow t\bar{t} \rightarrow tbH^\pm) \sim 80 \text{ pb}$ for $M_{H^\pm} \sim 150 \text{ GeV}$
 - $M_{H^\pm} \gtrsim m_t$: $\sigma(gb \rightarrow tH^\pm) \sim 1 \text{ pb}$ for $M_{H^\pm} \sim 300 \text{ GeV}$

 Preliminary

- A new mechanism (!): W - b scattering? W -Higgs fusion? : $qb \rightarrow q'H^+b$ in the MSSM S. Moretti, K. Odagiri PRD55 (1997) 5627, hep-ph/9611374



$M_{H^\pm} \lesssim m_t$: $\sigma(qb \rightarrow jbH^\pm)|_{\text{diagram b}} \sim 20 \text{ pb}$ for $M_{H^\pm} \sim 150 \text{ GeV}$

$M_{H^\pm} \gtrsim m_t$: $\sigma \lesssim 10^{-2} \text{ pb}$ for $M_{H^\pm} \gtrsim 300 \text{ GeV}$... why so small?



Contents

*We wish to study the role of W -Higgs fusion
in W - b scattering adopting general 2HDMs*

- 2HDM as a minimal model containing H^\pm
- Analytic understanding of the W - b scattering
- Results
- Summary

 2HDMs

- 2HDM : minimal model containing H^\pm [K.Cheung, JSL, P.Y.Tseng, JHEP 1401 \(2014\) 085, arXiv:1310.3937](#)

$$\begin{aligned}
 V = & -\mu_1^2(\Phi_1^\dagger \Phi_1) - \mu_2^2(\Phi_2^\dagger \Phi_2) - m_{12}^2(\Phi_1^\dagger \Phi_2) - m_{12}^{*2}(\Phi_2^\dagger \Phi_1) \\
 & + \lambda_1(\Phi_1^\dagger \Phi_1)^2 + \lambda_2(\Phi_2^\dagger \Phi_2)^2 + \lambda_3(\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4(\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) \\
 & + \frac{\lambda_5}{2}(\Phi_1^\dagger \Phi_2)^2 + \frac{\lambda_5^*}{2}(\Phi_2^\dagger \Phi_1)^2 + \lambda_6(\Phi_1^\dagger \Phi_1)(\Phi_1^\dagger \Phi_2) + \lambda_6^*(\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_1) \\
 & + \lambda_7(\Phi_2^\dagger \Phi_2)(\Phi_1^\dagger \Phi_2) + \lambda_7^*(\Phi_2^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1)
 \end{aligned}$$

$$\Phi_1 = \left(\begin{array}{c} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \phi_1^0 + ia_1) \end{array} \right); \quad \Phi_2 = e^{i\xi} \left(\begin{array}{c} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \phi_2^0 + ia_2) \end{array} \right)$$

♠ 2HDMs

- The 13 parameters of 2HDM

$$\begin{aligned} & v, \tan \beta, |m_{12}|; \\ & \lambda_1, \lambda_2, \lambda_3, \lambda_4, |\lambda_5|, |\lambda_6|, |\lambda_7|; \\ & \phi_5 + 2\xi, \phi_6 + \xi, \phi_7 + \xi, \text{sign}[\cos(\phi_{12} + \xi)] \end{aligned}$$

with $m_{12}^2 = |m_{12}|^2 e^{i\phi_{12}}$ and $\lambda_{5,6,7} = |\lambda_{5,6,7}| e^{i\phi_{5,6,7}}$

- $\mu_{1,2}^2$ are replaced with v and $\tan \beta$ through the CP-even tadpole conditions
- $\sin(\phi_{12} + \xi)$ is fixed by the CP-odd tadpole condition

One may take the convention with $\xi = 0$ without loss of generality.

 2HDMs

- The 3×3 mass matrix in $(\phi_1^0, \phi_2^0, a)^T$ basis

$$\mathcal{M}_0^2 = M_A^2 \begin{pmatrix} s_\beta^2 & -s_\beta c_\beta & 0 \\ -s_\beta c_\beta & c_\beta^2 & 0 \\ 0 & 0 & 1 \end{pmatrix} + \mathcal{M}_\lambda^2$$

$$\frac{\mathcal{M}_\lambda^2}{v^2} = \begin{pmatrix} 2\lambda_1 c_\beta^2 + \Re(\lambda_5 e^{2i\xi}) s_\beta^2 & \lambda_{34} c_\beta s_\beta + \Re(\lambda_6 e^{i\xi}) c_\beta^2 & -\frac{1}{2} \Im(\lambda_5 e^{2i\xi}) s_\beta \\ +2\Re(\lambda_6 e^{i\xi}) s_\beta c_\beta & +\Re(\lambda_7 e^{i\xi}) s_\beta^2 & -\Im(\lambda_6 e^{i\xi}) c_\beta \\ \lambda_{34} c_\beta s_\beta + \Re(\lambda_6 e^{i\xi}) c_\beta^2 & 2\lambda_2 s_\beta^2 + \Re(\lambda_5 e^{2i\xi}) c_\beta^2 & -\frac{1}{2} \Im(\lambda_5 e^{2i\xi}) c_\beta \\ +\Re(\lambda_7 e^{i\xi}) s_\beta^2 & +2\Re(\lambda_7 e^{i\xi}) s_\beta c_\beta & -\Im(\lambda_7 e^{i\xi}) s_\beta \\ -\frac{1}{2} \Im(\lambda_5 e^{2i\xi}) s_\beta & -\frac{1}{2} \Im(\lambda_5 e^{2i\xi}) c_\beta & 0 \\ -\Im(\lambda_6 e^{i\xi}) c_\beta & -\Im(\lambda_7 e^{i\xi}) s_\beta & \end{pmatrix}$$

with $\lambda_{34} = \lambda_3 + \lambda_4$, $v = g M_W / 2$, $a = -s_\beta a_1 + c_\beta a_2$, $H^+ = -s_\beta \phi_1^+ + c_\beta \phi_2^+$,

... and

$$\begin{aligned}
 M_A^2 &= M_{H^\pm}^2 + \frac{1}{2}\lambda_4 v^2 - \frac{1}{2}\operatorname{Re}(\lambda_5 e^{2i\xi})v^2 \\
 M_{H^\pm}^2 &= \frac{\operatorname{Re}(m_{12}^2 e^{i\xi})}{c_\beta s_\beta} - \frac{v^2}{2c_\beta s_\beta} [\lambda_4 c_\beta s_\beta + c_\beta s_\beta \operatorname{Re}(\lambda_5 e^{2i\xi}) \\
 &\quad + c_\beta^2 \operatorname{Re}(\lambda_6 e^{i\xi}) + s_\beta^2 \operatorname{Re}(\lambda_7 e^{i\xi})]
 \end{aligned}$$

- Diagonalization: $(\phi_1^0, \phi_2^0, a)_\alpha^T = O_{\alpha i} (H_1, H_2, H_3)_i^T$ with $O^T \mathcal{M}_0^2 O = \operatorname{diag}(M_{H_1}^2, M_{H_2}^2, M_{H_3}^2)$

$$O = \begin{pmatrix} O_{\phi_1 1} & O_{\phi_1 2} & O_{\phi_1 3} \\ O_{\phi_2 1} & O_{\phi_2 2} & O_{\phi_2 3} \\ O_{a 1} & O_{a 2} & O_{a 3} \end{pmatrix} \xrightarrow{\text{CPC with } H_3 = A} \begin{pmatrix} -\sin \alpha & \cos \alpha & 0 \\ \cos \alpha & \sin \alpha & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- Decoupling limit: $\sin \alpha \rightarrow -\cos \beta$, $\cos \alpha \rightarrow \sin \beta$

 2HDMs

- After identifying the Yukawa couplings by

$$h_u = \frac{\sqrt{2}m_u}{v} \frac{1}{s_\beta}; \quad h_d = \frac{\sqrt{2}m_d}{v} \frac{1}{\eta_1^d c_\beta + \eta_2^d s_\beta}; \quad h_l = \frac{\sqrt{2}m_l}{v} \frac{1}{\eta_1^l c_\beta + \eta_2^l s_\beta},$$

one can easily obtain the following Higgs-fermion-fermion interactions

$$\begin{aligned} -\mathcal{L}_{H_i \bar{f} f} &= \frac{m_u}{v} \left[\bar{u} \left(\frac{O_{\phi_2 i}}{s_\beta} - i \frac{c_\beta}{s_\beta} O_{ai} \gamma_5 \right) u \right] H_i \\ &+ \frac{m_d}{v} \left[\bar{d} \left(\frac{\eta_1^d O_{\phi_1 i} + \eta_2^d O_{\phi_2 i}}{\eta_1^d c_\beta + \eta_2^d s_\beta} - i \frac{\eta_1^d s_\beta - \eta_2^d c_\beta}{\eta_1^d c_\beta + \eta_2^d s_\beta} O_{ai} \gamma_5 \right) d \right] H_i \\ &+ \frac{m_l}{v} \left[\bar{l} \left(\frac{\eta_1^l O_{\phi_1 i} + \eta_2^l O_{\phi_2 i}}{\eta_1^l c_\beta + \eta_2^l s_\beta} - i \frac{\eta_1^l s_\beta - \eta_2^l c_\beta}{\eta_1^l c_\beta + \eta_2^l s_\beta} O_{ai} \gamma_5 \right) l \right] H_i \end{aligned}$$

and

$$\begin{aligned}
-\mathcal{L}_{H^\pm \bar{u}d} = & -\frac{\sqrt{2}m_u}{v} \left(\frac{c_\beta}{s_\beta} \right) \bar{u} P_L d H^+ - \frac{\sqrt{2}m_d}{v} \left(\frac{\eta_1^d s_\beta - \eta_2^d c_\beta}{\eta_1^d c_\beta + \eta_2^d s_\beta} \right) \bar{u} P_R d H^+ \\
& - \frac{\sqrt{2}m_l}{v} \left(\frac{\eta_1^l s_\beta - \eta_2^l c_\beta}{\eta_1^l c_\beta + \eta_2^l s_\beta} \right) \bar{\nu} P_R l H^+ + \text{h.c.}
\end{aligned}$$

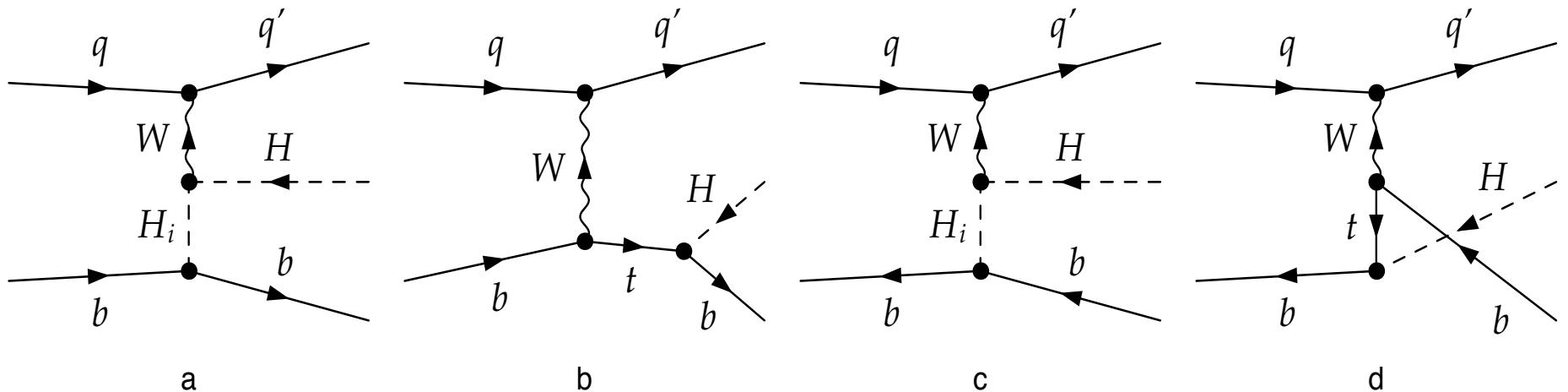
- Classification of 2HDMs satisfying the Glashow-Weinberg condition which guarantees the absence of tree-level FCNC

	2HDM I	2HDM II	2HDM III	2HDM IV
η_1^d	0	1	0	1
η_2^d	1	0	1	0
η_1^l	0	1	1	0
η_2^l	1	0	0	1

♠ *Process*

- The $2 \rightarrow 3$ processes $qb \rightarrow q'H^+b$ and $q\bar{b} \rightarrow q'H^+\bar{b}$ with $(q, q') = (u, d), (c, s)$.

The processes with $(\bar{q}, \bar{q}') = (\bar{d}, \bar{u}), (\bar{s}, \bar{c})$ are understood.

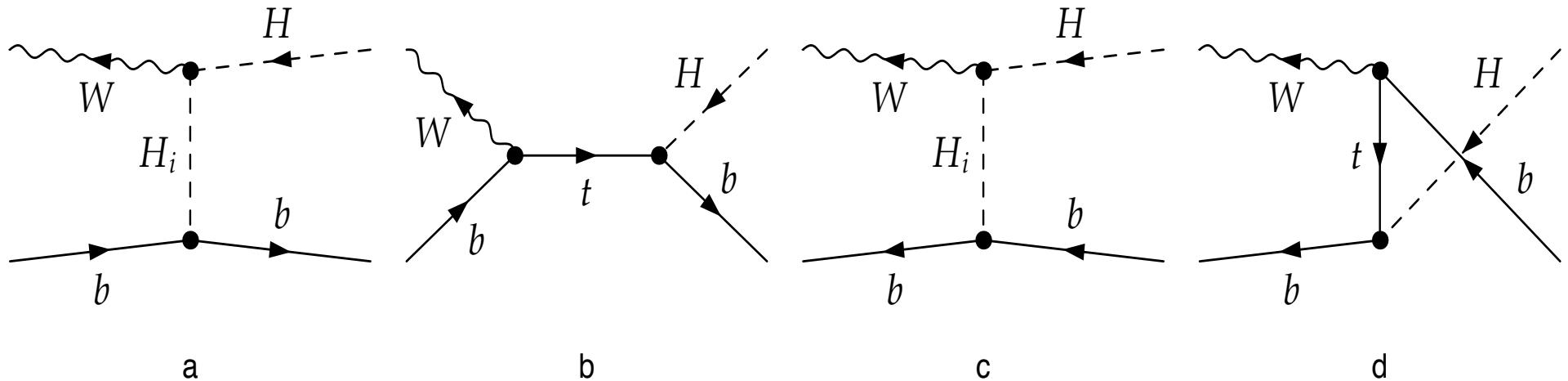


- a, c : t -channel H_i exchanges $\leftarrow W$ - H_i fusion into H^+
- b : s -channel top exchange \leftarrow single top^(*) production decaying into $H^+ b$
- d : u -channel top exchange

♠ *Process*

- The $2 \rightarrow 2$ subprocesses in the effective W approximation:

$$W^+(q_1) b(p_1) \rightarrow H^+(q_2) b(p_2); \quad W^+(q_1) \bar{b}(p_1) \rightarrow H^+(q_2) \bar{b}(p_2)$$



- (b) : $s = (p_1 + q_1)^2 = (p_2 + q_2)^2$
- $(a), (c)$: $t = (p_1 - p_2)^2 = (q_2 - q_1)^2$
- (d) : $u = (p_1 - q_2)^2 = (p_2 - q_1)^2$

 *Process*

- The relevant interactions:

$$\mathcal{L}_{H_i \bar{b} b} = -\frac{g m_b}{2 m_W} \bar{b} (g_i^S + i g_i^P \gamma_5) b H_i ,$$

$$\mathcal{L}_{H^\pm t b} = +\frac{g m_b}{\sqrt{2} m_W} \bar{b} (c_L P_L + c_R P_R) t H^- + \text{h.c.} ,$$

$$\mathcal{L}_{W^\pm t b} = -g/\sqrt{2} (\bar{t} \gamma_\mu P_L b) W^{+\mu} + \text{h.c.} ,$$

$$\mathcal{L}_{H_i H^\pm W^\pm} = -\frac{g}{2} (S_i + i P_i) \left[H^- \left(i \overset{\leftrightarrow}{\partial}_\mu \right) H_i \right] W^{+\mu} + \text{h.c.}$$

- Type-independent couplings:

$$S_i = c_\beta O_{\phi_2 i} - s_\beta O_{\phi_1 i} , \quad P_i = O_{a i} ,$$

- Types II and IV

$$c_L = \tan \beta, \quad c_R = \frac{m_t}{m_b} \frac{1}{\tan \beta}; \quad g_i^S = \frac{O_{\phi_1 i}}{c_\beta}, \quad g_i^P = -\tan \beta O_{ai}$$

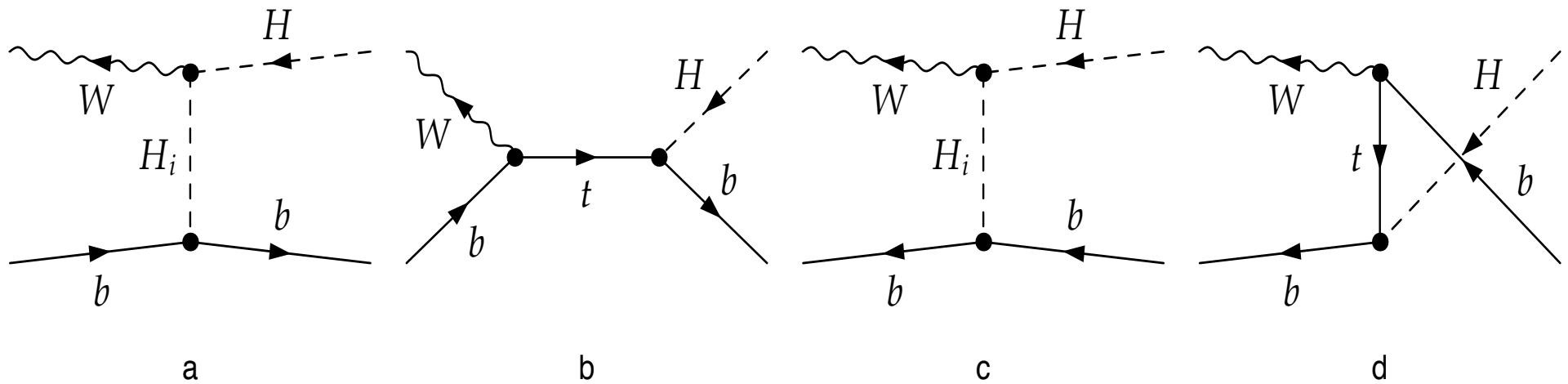
- Types I and III

$$c_L = -\frac{1}{\tan \beta}, \quad c_R = \frac{m_t}{m_b} \frac{1}{\tan \beta}; \quad g_i^S = \frac{O_{\phi_2 i}}{s_\beta}, \quad g_i^P = \frac{O_{ai}}{\tan \beta}$$

 *Process*

- The $2 \rightarrow 2$ subprocesses in the effective W approximation:

$$W^+(q_1) b(p_1) \rightarrow H^+(q_2) b(p_2); \quad W^+(q_1) \bar{b}(p_1) \rightarrow H^+(q_2) \bar{b}(p_2)$$



$$\mathcal{M}_{(a)}^{H_i} = -\frac{g^2 m_b}{4m_W(t - M_{H_i}^2)} (S_i + iP_i) (q_2 + p_{H_i})^\mu \epsilon_\mu(q_1) [\bar{u}(p_2) (g_i^S + ig_i^P \gamma_5) u(p_1)]$$

$$\mathcal{M}_{(b)} = -\frac{g^2 m_b C_v}{2m_W(s - m_t^2)} [c_L \bar{u}(p_2) \not{p}_t \not{\epsilon}(q_1) P_L u(p_1) + c_R m_t \bar{u}(p_2) \not{\epsilon}(q_1) P_L u(p_1)]$$

$\epsilon^\mu(q_1)$ denotes the polarization vector of W^+ boson

- In the high-energy limit, $s, |t|, |u| \gg m_W^2, m_t^2, M_{H_i}^2, M_{H^\pm}^2$, we find that

$$\begin{aligned} \mathcal{M} = \mathcal{M}_{(b)} + \sum_i \mathcal{M}_{(a)}^{H_i} &\approx \frac{g^2 m_b}{4m_W^2} \left\{ \left[\sum_i (S_i g_i^S - P_i g_i^P) + i \sum_i (S_i g_i^P + P_i g_i^S) \right] \bar{u}(p_2) P_R u(p_1) \right. \\ &+ \left. \left[\left(2c_L + \sum_i (S_i g_i^S + P_i g_i^P) \right) + i \sum_i (-S_i g_i^P + P_i g_i^S) \right] \bar{u}(p_2) P_L u(p_1) \right\} \end{aligned}$$

where we have taken the longitudinally polarized W or $\epsilon^\mu(q_1) \approx q_1^\mu/m_W = (p_t^\mu - p_1^\mu)/m_W$ with $p_t^2 = s$ and $p_{H_i}^2 = t$.

- The amplitude squared in the high-energy limit:

$$\begin{aligned} \overline{|\mathcal{M}|^2} &\propto \left\{ \left| 2c_L + \sum_i (S_i g_i^S + P_i g_i^P) \right|^2 + \left| \sum_i (S_i g_i^S - P_i g_i^P) \right|^2 \right. \\ &+ \left. \left| \sum_i (-S_i g_i^P + P_i g_i^S) \right|^2 + \left| \sum_i (S_i g_i^P + P_i g_i^S) \right|^2 \right\} (-t) \end{aligned}$$

 *Process*

- *Sum rules required by the absence of unitarity-breaking terms:*

$$2c_L + \sum_i (S_i g_i^S + P_i g_i^P) = 0, \quad \sum_i S_i g_i^S = \sum_i P_i g_i^P,$$

$$\sum_i S_i g_i^P = \sum_i P_i g_i^S = 0$$

- Type II and IV: $c_L = \tan \beta$

$$\sum_i S_i g_i^S = \sum_i (O_{\phi_2 i} O_{\phi_1 i} - \tan \beta O_{\phi_1 i}^2) = -\tan \beta,$$

$$\sum_i P_i g_i^P = -\tan \beta \sum_i O_{ai}^2 = -\tan \beta, \quad \sum_i S_i g_i^P = \sum_i P_i g_i^S = 0$$

- Type I and III: $c_L = -1/\tan \beta$

$$\sum_i S_i g_i^S = \sum_i (O_{\phi_2 i}^2 / \tan \beta - O_{\phi_1 i} O_{\phi_2 i}) = 1/\tan \beta,$$

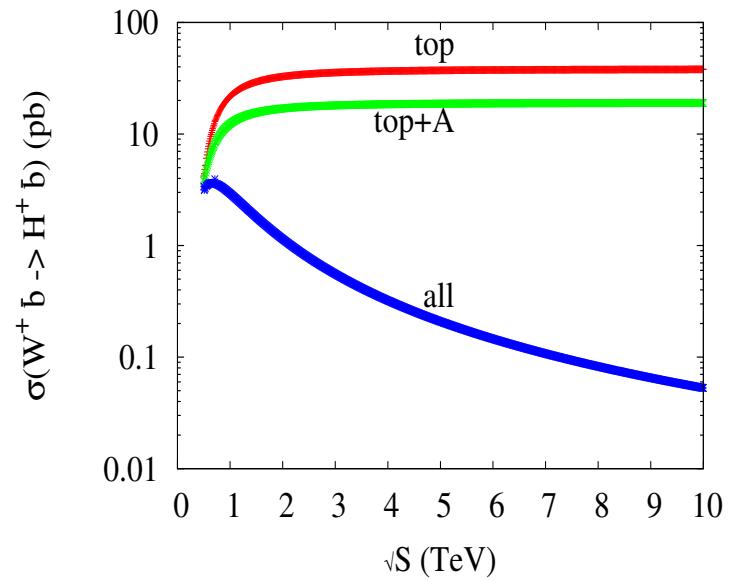
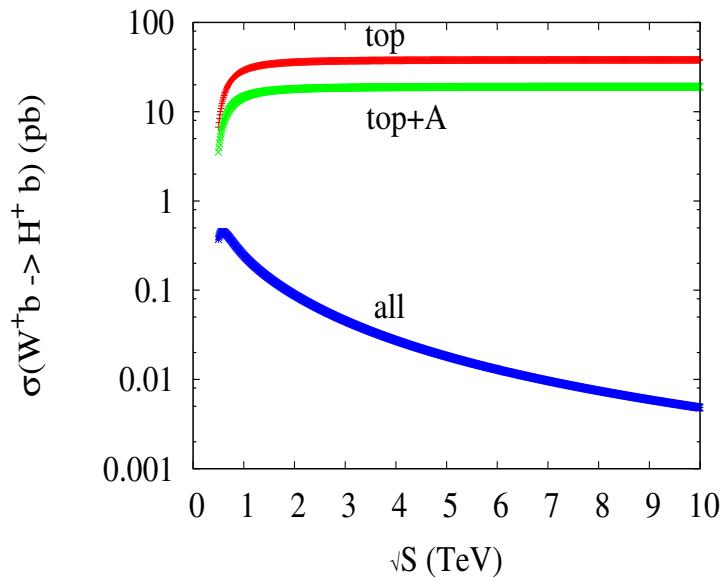
$$\sum_i P_i g_i^P = \sum_i O_{ai}^2 / \tan \beta = 1/\tan \beta, \quad \sum_i S_i g_i^P = \sum_i P_i g_i^S = 0$$

 *Process*

- Numerical example: MSSM in the CP conserving \oplus decoupling limit:
 - $c_L = \tan \beta$ (Type II)
 - $H_1 = h, H_2 = H, H_3 = A$
 - $S_h = \cos(\beta - \alpha), S_H = -\sin(\beta - \alpha), P_A = 1$ with $P_h = P_H = S_A = 0$
 - $S_h \rightarrow 0, S_H \rightarrow -1; g_H^S \rightarrow \tan \beta, g_A^P \rightarrow -\tan \beta$

$$\sigma(W^+ b \rightarrow H^+ b) \propto |2c_L + S_H g_H^S + P_A g_A^P|^2 + |S_H g_H^S - P_A g_A^P|^2$$

$$\sigma(W^+ b \rightarrow H^+ b) \propto |2c_L + S_H g_H^S + P_A g_A^P|^2 + |S_H g_H^S - P_A g_A^P|^2$$



- $\tan \beta = 30, M_A = 400$ GeV
- $\sigma(W^+ b \rightarrow H^+ b)|_{t \text{ only}} \propto 4 \tan^2 \beta$
- $\sigma(W^+ b \rightarrow H^+ b)|_{t+H \text{ only}} = \sigma(W^+ b \rightarrow H^+ b)|_{t+A \text{ only}} \propto 2 \tan^2 \beta$
- $\sigma(W^+ b \rightarrow H^+ b)|_{t+H+A} \propto \mathcal{O}(m_t^2/s, M_H^2/|t|, m_t^2/|u|)$

 *Process*

- Comments:
 - The b -initiated process for production of H^+ in $qb \rightarrow qH^+b$ suffers from very strong cancellations between the top and the W - H_i diagrams and among the W - H_i diagrams
 - While, for the \bar{b} -initiated process, the cancellation is less severe
 - The strong cancellation is dictated by the absence of the unitarity-breaking terms expressed by the sum rules
 - The cross section can be enhanced if we can avoid the cancellations: (i) sizable hierarchy between M_A and M_H , (ii) a 2HDM is not an UV complete theory, and/or ...

♠ Results

- We consider 2HDMs without CP violation, identifying $H_1 = h$, $H_2 = H$, $H_3 = A$ with $M_h = 125$ GeV
- Couplings:
 - $S_1 = S_h = c_\beta O_{\phi_2 1} - s_\beta O_{\phi_1 1} = \cos(\beta - \alpha)$
 - $S_2 = S_H = c_\beta O_{\phi_2 2} - s_\beta O_{\phi_1 2} = -\sin(\beta - \alpha)$
 - $P_3 = P_A = O_{a3} = 1$
 - $P_1 = P_2 = S_3 = 0$ (CPC)

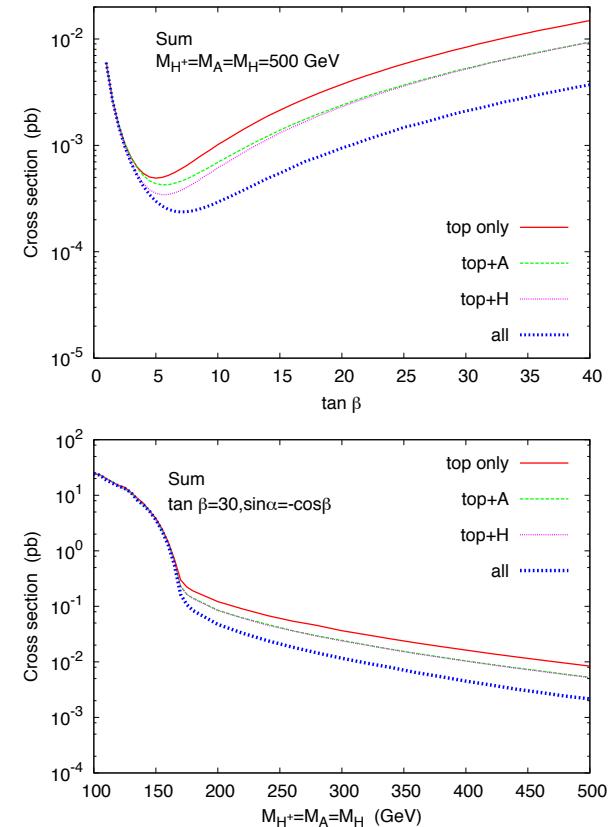
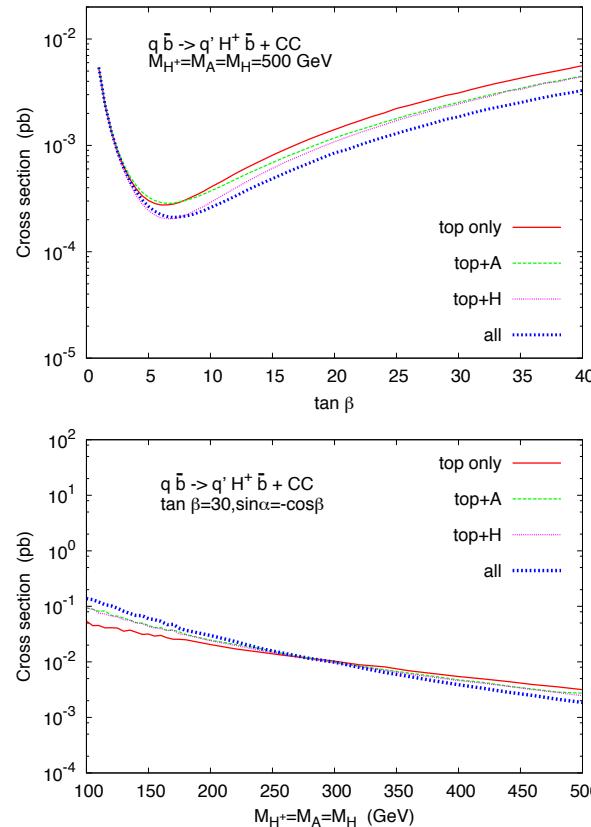
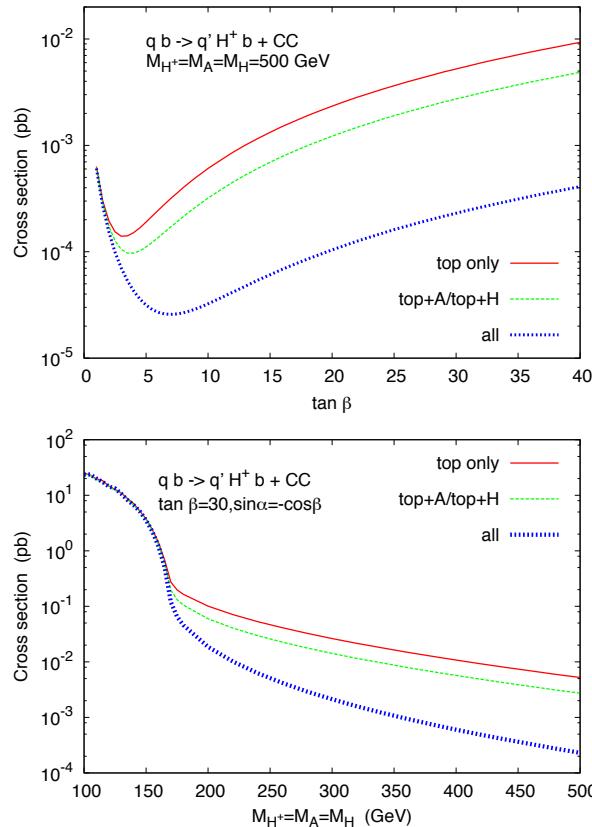
- Yukawa couplings: $gm_b/\sqrt{2}M_W \times \cdots (h, H, A)$, $g/\sqrt{2}M_W \times \cdots (H^\pm)$

	Type I, III	Type II, IV
$h b \bar{b}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$
$H b \bar{b}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$
$A b \bar{b}$	$+\cot \beta$	$-\tan \beta$
$H^- t \bar{b}$	$-\frac{m_b}{\tan \beta} P_L + \frac{m_t}{\tan \beta} P_R$	$m_b \tan \beta P_L + \frac{m_t}{\tan \beta} P_R$

- Free parameters: $\tan \beta$, M_H , M_A , M_{H^\pm} , $\sin \alpha$. We are taking the decoupling $\sin \alpha = -\cos \beta$ mostly
- We have checked the results of our calculation against those obtained by MadGraph, found an excellent agreement

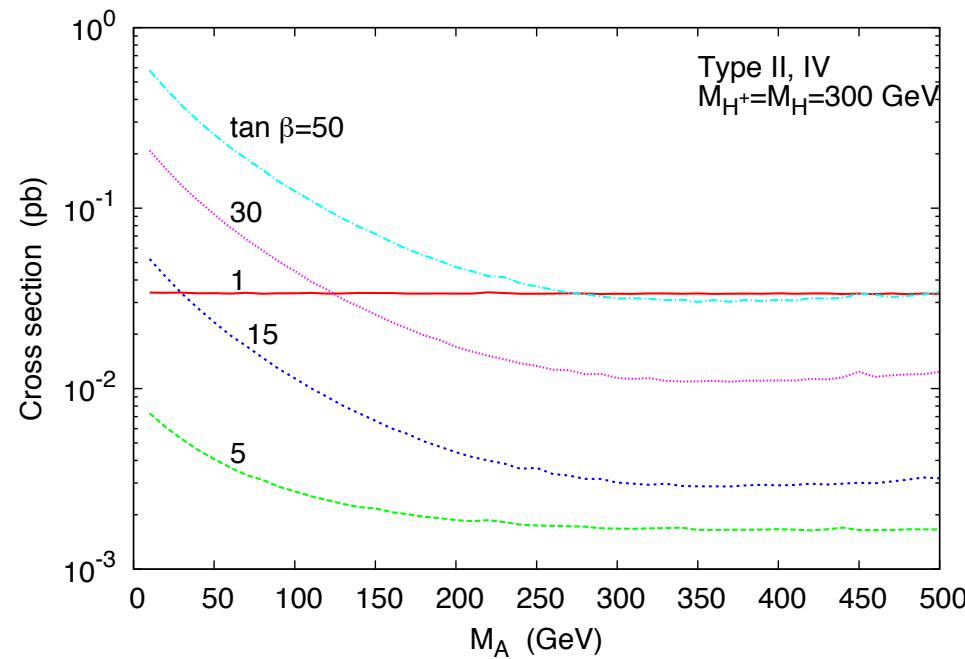
♠ Results

- Type II $\sigma(pp \rightarrow jH^\pm b/\bar{b})$ at LHC-14: $\tan\beta$ (Upper) ; $M_A = M_H = M_{H^\pm}$ (Lower) ; $qb \rightarrow q'H^+b + c.c.$ (left), $q\bar{b} \rightarrow q'H^+\bar{b} + c.c.$ (middle), total sum (right)



♠ Results

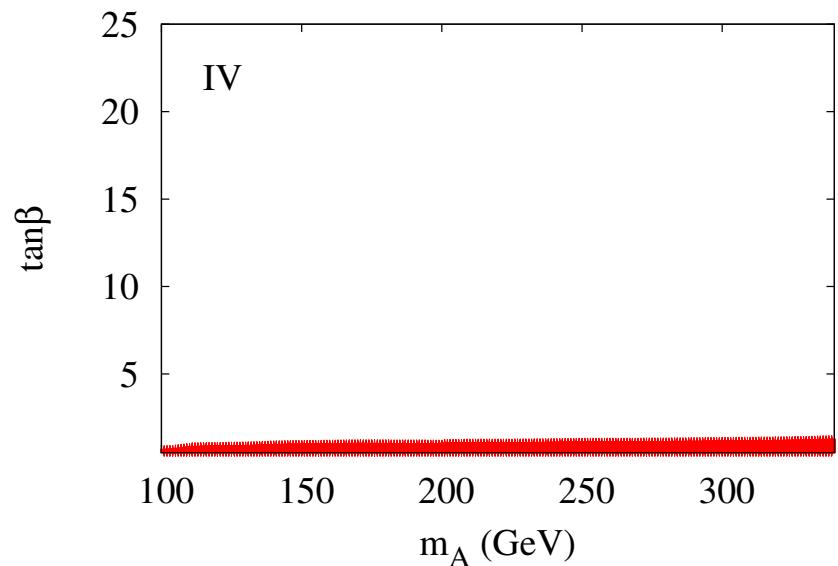
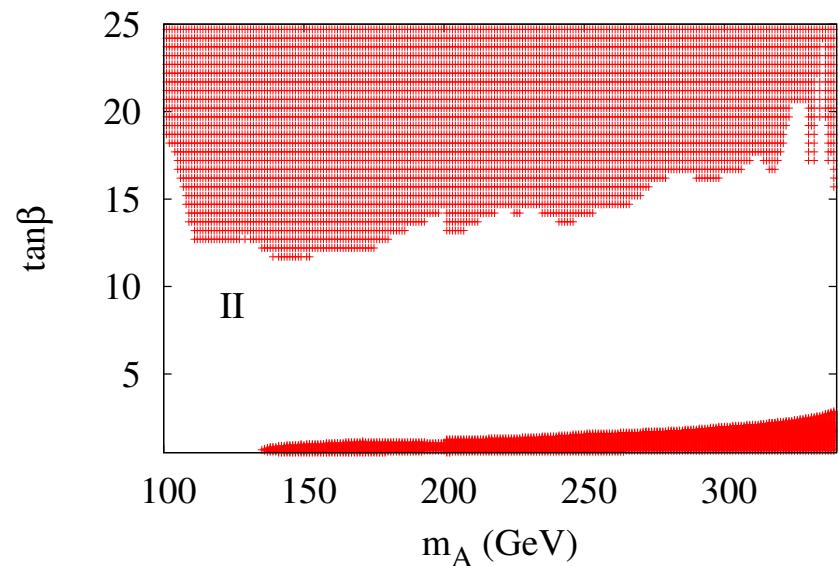
- Type II, IV: $M_A \neq M_H = M_{H^\pm}$



The larger cross section for the larger values of $\tan \beta$ when $M_A \leq M_H = M_{H^\pm}$

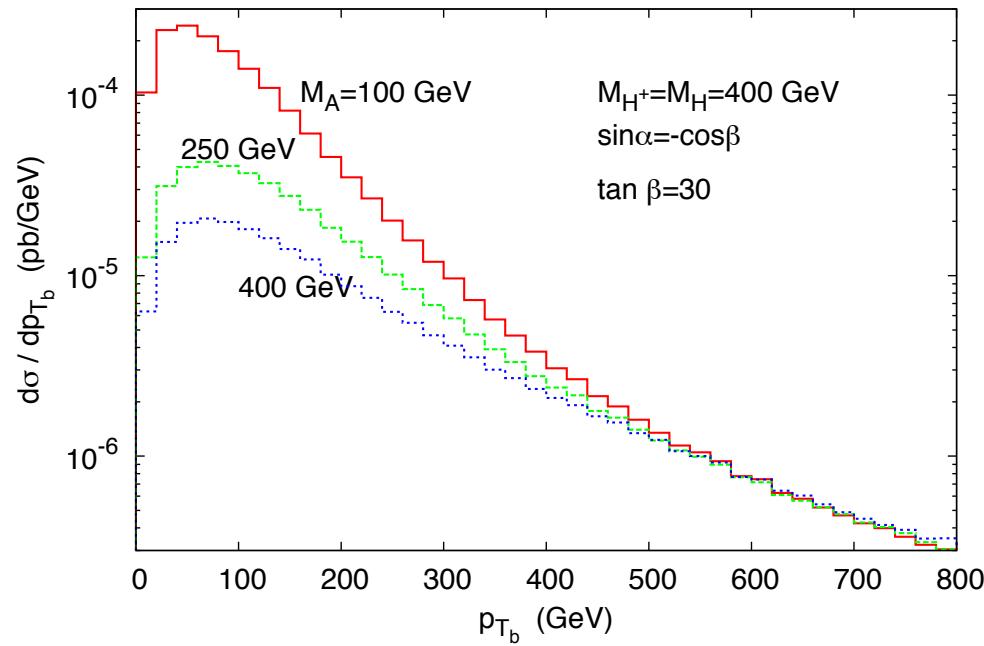
♠ Results

- Constraints from ATLAS : $gg \rightarrow A \rightarrow \tau^+ \tau^-$ JHEP **1411**, 056 (2014), [arXiv:1409.6064]



♠ Results

- Discriminating W^\pm -Higgs fusion from the top-exchange processes



 *Summary*

- The b -initiated process for production of H^+ in $qb \rightarrow qH^+b$ suffers from a very strong cancellation between the top diagram and the $W\text{-}H_i$ diagrams
- The strong cancellation is dictated by the absence of the unitarity-breaking terms and we find the sum rules expressed by the relevant Higgs couplings
- For $M_{H^\pm} \leq m_t - m_b$ the top diagram completely dominates through the s -channel single-top production. However, when $M_{H^\pm} > m_t - m_b$, the $W\text{-}H_i$ fusion diagrams also contribute
- The process $pp \rightarrow jH^\pm b/\bar{b}$ would be more interesting for type II and IV (especially type IV) : $\sigma \sim O(100 - 300)$ fb for $\tan\beta = 30 - 50$ and $M_A = 50 - 100$ GeV
- One may make use of the special kinematics, e.g, the p_{Tb} distribution, to discriminate between the top and the $W\text{-}H_i$ fusion diagrams