# A Classification of Simple W' Models 

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## Life with Higgs

Higgs was discovered in 2012

- consistent with the SM prediction
- no significant deviations so far

Higgs is still mysterious

- hierarchy problem? ( $\mathrm{V}_{\mathrm{EW}} \ll$ m Planck ?)
- Yukawa interaction? ( $\mathrm{y}_{\mathrm{up}} \ll \mathrm{Y}_{\text {top }}$ ?)
- origin of the potential?
- elementary or composite?
- only one scalar?
- ...


## Spin-I particle

## Composite Higgs

- a solution of the hierarchy problem
- many other composite particles

Higgs boson

unknown particles
unknown particles

Spin-1 new particles ( $\mathbf{V}^{\prime}=W^{\prime}, Z^{\prime}$ )

new particle

V' also appears in different context

- extension of EW gauge symmetry (Left-Right symmetric model, $\cdot \cdots$ )
- some kind of GUT models
- Extra-dimension (KK modes)
- ...


## too many V' models ...

Q. What is an efficient way to treat many models?
A. Use effective theory [Pappadopulo et.al (2014)]

- three important parameters ( $\mathrm{g}_{\mathrm{v}^{\prime} f f}, \mathrm{~g}_{\mathrm{v}^{\prime} \mathrm{vv}}, \mathrm{m}_{\mathrm{v}^{\prime}}$ )
- $\mathrm{V}^{\prime}=\mathrm{SU}(2) \mathrm{L}$ triplet vector field
Q. If $\mathrm{V}^{\prime}$ is discovered at the LHC, does effective theory satisfy us?
A. No, we need to find the model
Q. But too many models … Any efficient ways?
A. OK, classify $\mathrm{V}^{\prime}$ setup.


## What is the main decay mode of $V$ '?

parametrize couplings

$$
\begin{aligned}
g_{V^{\prime} f f} & =-\xi_{f} g_{V f f}, \\
g_{V^{\prime} V V} & =\xi_{V} \frac{m_{V}^{2}}{m_{V^{\prime}}^{2}} g_{V V V}
\end{aligned}
$$

ratio of $\Gamma$

$$
\frac{\Gamma\left(V^{\prime} \rightarrow f f\right)}{\Gamma\left(V^{\prime} \rightarrow V V\right)} \simeq 4 N_{c} \frac{\xi_{f}^{2}}{\xi_{V}^{2}}
$$

main decay mode is determined by the relation between $\boldsymbol{\xi}_{\mathrm{f}}$ and $\boldsymbol{\xi}_{\mathrm{V}}$

- For $\boldsymbol{\xi}_{\mathrm{f}}>\boldsymbol{\xi}_{\mathrm{v}}$ or $\boldsymbol{\xi}_{\mathrm{f}} \sim \boldsymbol{\xi}_{\mathrm{v}}, \mathrm{V}^{\prime}$ mainly decay to fermions
- For $\xi_{f}<\xi_{\mathrm{v}}$, $\quad \mathrm{V}^{\prime}$ mainly decay to bosons
perturbative unitarity helps us to find the relation between $\xi_{f}$ and $\xi_{v}$ without specifying any models


## Perturbative unitarity

processes and amplitude

- $\mathrm{ff} \rightarrow \mathrm{VV}$, ff $\rightarrow \mathrm{VV}^{\prime}$ ff $\rightarrow \mathrm{V}^{\prime} \mathrm{V}^{\prime} \quad \mathrm{Amp} \sim \mathbf{a} \mathrm{E}^{2}+\mathbf{b} \mathrm{E}^{1}+\cdots$
- $\mathrm{VV} \rightarrow \mathrm{VV}, \mathrm{VV} \rightarrow \mathrm{VV}^{\prime}, \cdots \quad \mathrm{Amp} \sim \mathrm{c} \mathrm{E}^{4}+\mathbf{d} \mathrm{E}^{2}+\cdots$
impose : $\mathbf{a}=\mathbf{b}=\mathbf{c}=\mathbf{d}=\mathbf{0}$
- example: a $=0$ leads $g_{V f f} g_{V^{\prime} f f}=g_{V f f} g_{V^{\prime} V V}+g_{V^{\prime} f f} g_{V^{\prime} V^{\prime} V}$,



## Perturbative unitarity (cont')

$\mathbf{V V} \rightarrow \mathbf{V V}, \mathbf{V V} \rightarrow \mathbf{V} \mathbf{V}^{\prime}, \mathbf{V V} \rightarrow \mathbf{V}^{\prime} \mathbf{V}^{\prime} \quad\left(A m p \sim \mathbf{c} E^{4}+\mathbf{d} E^{2}+\cdots\right)$

$h: \mathrm{SU}(2)$ singlet, $\Delta$ : triplet, $X$ : five-plet
example: d = $\mathbf{0}$ in $\mathbf{V V} \rightarrow \mathbf{V V}$ leads

$$
\left(3 m_{V}^{2}+m_{V^{\prime}}^{2}\right) g_{V^{\prime} V V V}-3 \sum_{k} m_{k}^{2} g_{V_{k} V V} g_{V^{\prime} V_{k} V}=\sum_{h} g_{V V h} g_{V V^{\prime} h}-\frac{5}{6} \sum_{X} g_{V V X} g_{V V^{\prime} X},
$$

## Perturbative unitarity (cont')

## we find various coupling relations

- quadratic equations for the couplings
- two solutions for the relation $\boldsymbol{\xi}_{f}$ and $\boldsymbol{\xi}_{\boldsymbol{v}}$

$$
\begin{aligned}
& g_{V^{\prime} f f}=-\xi_{f} g_{V_{f f},}, \\
& g_{V^{\prime} V V}=\xi_{V} \frac{m_{V}^{2}}{m_{V^{\prime}}^{2}} g_{V V V}
\end{aligned}
$$

In all scalars are $\mathbf{S U ( 2 )}$ singlet case
$\mathbf{V}^{\prime}$ decay to fermion

$$
\begin{array}{ll}
\xi_{V}=\frac{\xi_{f}}{1-\frac{m^{2}}{m_{W^{\prime}}^{2}}\left(1-\xi_{f}^{2}\right)} \simeq \xi_{f} & \frac{\Gamma\left(V^{\prime} \rightarrow f f\right)}{\Gamma\left(V^{\prime} \rightarrow V V\right)} \simeq 4 N_{c} \\
\xi_{V}=-\frac{1}{\xi_{f}} \frac{1}{1-\frac{m_{2}^{2}}{m_{W^{\prime}}^{2}}\left(1-\xi_{f}^{-2}\right)} \simeq-\frac{1}{\xi_{f}} & \frac{\Gamma\left(V^{\prime} \rightarrow f f\right)}{\Gamma\left(V^{\prime} \rightarrow V V\right)} \simeq 4 N_{c} \xi_{f}^{4}
\end{array}
$$

## $\xi_{v}$ vs $\xi_{f}$ (all scalars are $\mathbf{S U}(2)$ singlet)

$$
\xi_{V}=\frac{\xi_{f}}{1-\frac{m_{W}^{2}}{m_{W^{\prime}}^{2}}\left(1-\xi_{f}^{2}\right)} \simeq \xi_{f} \quad \quad \xi_{V}=-\frac{1}{\xi_{f}} \frac{1}{1-\frac{m_{W}^{2}}{m_{W^{\prime}}^{2}}\left(1-\xi_{f}^{-2}\right)} \simeq-\frac{1}{\xi_{f}}
$$




## two classes of V' models

We found two classes of models

- type-F: $\xi_{\mathrm{V}} \sim \xi_{\mathrm{f}}, \Gamma\left(\mathrm{V}^{\prime} \rightarrow \mathrm{ff}\right) \gg \Gamma\left(\mathrm{V}^{\prime} \rightarrow \mathrm{VV}\right)$
- type-B: $\xi_{V} \sim 1 / \xi_{f}, \Gamma\left(V^{\prime} \rightarrow f f\right) \ll \Gamma\left(V^{\prime} \rightarrow V V\right)$
$g_{V^{\prime} f f}=-\xi_{f} g_{V f f}$,
$g_{V^{\prime} V V}=\xi_{V} \frac{m_{V}^{2}}{m_{V^{\prime}}^{2}} g_{V V V}$

This classification also valid in systems with triplet/five-plet scalars

This is model independent result, but

- specific models are suitable for the LHC pheno.
- next step is find benchmark models for each of types


## type-F example : HVT model A

$\operatorname{SU}(2)_{0} \times \operatorname{SU}(2)_{1} \times U(1)_{2} \rightarrow U(1)_{Q E D}$

|  | $\mathrm{SU}(2)$ | $\mathrm{SU}(2)$ | $\mathrm{U}(1)$ |
| :---: | :---: | :---: | :---: |
| $q$ | 2 | 1 | $1 / 6$ |
| $u$ | 1 | 1 | $2 / 3$ |
| $d$ | 1 | 1 | $-1 / 3$ |
| $\ell$ | 2 | 1 | $-1 / 2$ |
| $e$ | 1 | 1 | -1 |
| $H$ | 2 | 1 | $1 / 2$ |
| $H$ | 2 | 2 | 0 |



$$
H_{1}=\left(\begin{array}{cc}
v_{1}+h_{1}+i \pi_{1}^{0} & i \sqrt{2} \pi_{1}^{+} \\
i \sqrt{2} \pi_{1}^{-} & v_{1}+h_{1}-i \pi_{1}^{0}
\end{array}\right)
$$

$$
H_{2}=\frac{1}{\sqrt{2}}\binom{i \sqrt{2} \pi_{2}^{+}}{v_{2}+h_{2}-i \pi_{2}^{0}}
$$

## type-B example

TA - Kitano (2013)
$S U(2)_{0} \times S U(2)_{1} \times U(1)_{2} \rightarrow U(1)_{\text {QED }}$

|  | $\mathrm{SU}(2)$ | $\mathrm{SU}(2)$ | $\mathrm{U}(1)$ |
| :---: | :---: | :---: | :---: |
| $q$ | 2 | 1 | $1 / 6$ |
| $u$ | 1 | 1 | $2 / 3$ |
| $d$ | 1 | 1 | $-1 / 3$ |
| $\ell$ | 2 | 1 | $-1 / 2$ |
| $e$ | 1 | 1 | -1 |
| $H$ | 2 | 1 | $1 / 2$ |
| $H$ | 2 | 2 | 0 |
| $H$ | 1 | 2 | $1 / 2$ |



$$
H_{1}=\left(\begin{array}{cc}
v_{1}+h_{1}+i \pi_{1}^{0} & i \sqrt{2} \pi_{1}^{+} \\
i \sqrt{2} \pi_{1}^{-} & v_{1}+h_{1}-i \pi_{1}^{0}
\end{array}\right) \quad H_{2}=\frac{1}{\sqrt{2}}\binom{i \sqrt{2} \pi_{2}^{+}}{v_{2}+h_{2}-i \pi_{2}^{0}} \quad H_{3}=\frac{1}{\sqrt{2}}\binom{i \sqrt{2} \pi_{3}^{+}}{v_{3}+h_{3}-i \pi_{3}^{0}}
$$

## what makes difference?

type-F

type-B
Note:
$V^{\prime} V V$ coupling $\sim V^{\prime} \pi \vee \pi \vee$ coupling


## what makes difference?

type-F type-B

## Note:

$V^{\prime} V V$ coupling $\sim V^{\prime} \pi \vee \pi_{V}$ coupling

assume $V^{\prime} \sim \operatorname{SU}(2)_{1}$
(this is true if $\mathrm{g}_{1} \gg 1$ )

## what makes difference?

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type-F type-B
```



## V' coupling to $\pi \mathrm{v}$ is suppressed

## what makes difference?

type-F type-B

Note:
$\pi v$ should be here $\quad V^{\prime} V V$ coupling $\sim V^{\prime} \pi \vee \pi v$ coupling
$\pi \mathrm{v}$ ' should be here
assume $V^{\prime} \sim \operatorname{SU}(2)_{1}$ (this is true if $\mathrm{g}_{1} \gg 1$ )
$\pi v$ ' are mixture of $\mathrm{H}_{1}$ and $\mathrm{H}_{2}$ $\pi \mathrm{v}$ are mixture of $\mathrm{H}_{1} \mathrm{H}_{2}$ and $\mathrm{H}_{3}$

V' coupling to $\pi \mathrm{v}$ is suppressed
V' directly couple to $\pi \mathrm{v}$
$g_{V^{\prime} V V} \ll g_{V^{\prime} V V}$

## LHC bounds



## Summary

- there are many models with spin- 1 new particles ( $\mathrm{V}^{\prime}$ )
* composite Higgs models
* extra-dimension models
* GUT
^ $\cdots$
- two types of $\mathbf{V}^{\prime}$
$\star$ type-F: $\mathrm{V}^{\prime} \rightarrow$ ff is main decay mode
$\star$ type- $\mathrm{B}: \mathrm{V}^{\prime} \rightarrow \mathrm{VV}$ is main decay mode
- we showed the clear difference of the two types
- we showed benchmark models for each type

